

Statistical graphics

1 Data sets are prevalent, from TV news to academic papers. A data set often contains at least
2 hundreds of data points, and it is important to quickly extract meanings from the data. Group
3 statistics are often the critical information and need to be visualized.

4 A common message to be extrapolated from a data set is whether the groups examined are
5 different. The average value of each group is an intuitive and widely used group statistic. Therefore,
6 data graphs often represent the average values. By directly comparing the average values, the viewers
7 can quickly visualize how similar or different the groups are. In academia, bar graphs are normally
8 used to represent and compare the group averages. There are advantages in using bar graphs to
9 represent data. For example, higher values are represented by taller bars, consistent with the intuitive
10 representation of intensity. There are also disadvantages in using bar graphs. For example, height
11 differences in spatially separate bars are less salient (Nothelfer & Franconeri, 2017). The reason is
12 that the spatial separation of the bars discourages the viewers to group the bars and directly compare
13 them. The choice of the graph type ultimately depends on the most important message. If the
14 message is the differences between the groups, then the bars need to be at least physically close, so
15 that they can be visually grouped and easily compared. If the message is the specific value of each
16 group, the bars need to be separated. That way, the average value of each group can be quickly
17 perceived against the y-axis.

18 The representation of average values does miss a few important statistics of the data set.
19 While variance of each group can be represented by adding error bars, it is difficult to simultaneously
20 present other missing statistics such as mode, distribution, and range. An easy fix would be to
21 represent the individual data points on the graph. This is especially effective as people can quickly
22 extract the average value of an object set through ensemble encoding (Chong & Treisman, 2005).
23 However, this method is rather uncommon in academia because: 1) Larger data sets cannot be clearly
24 represented in a size-limited figure. 2) While people can quickly estimate the average, it is hard for
25 them to extract the group variance and infer whether two groups are statistically different (Pak,
26 Hutchinson, & Turk-Browne, 2014). Therefore, representing individual data points should be
27 considered in cases when statistical inferences are unimportant.

28 In addition to representing the group statistics, the groups also need to be easily
29 distinguishable. A simple group-wise comparison is clear using bar graphs, as each group is
30 represented by a separate bar. However, studies examining multiple interacting factors (e.g., gender,
31 before/after treatment, health) need to apply multiple feature dimensions to the figures. Color is an
32 adequate tool to represent different categories (Wong, 2010) as it has three dimensions: hue,
33 brightness, and saturation (Hurvich & Jameson, 1955). However, when there are more than three
34 factors, features such as texture, shape must also be considered in visualizing the categories.

35 This essay examined how group statistics can be effectively visualized. The specific method
36 of visualization depends on the most important message to be conveyed. When factors such as
37 statistical significance and individual performance are both important, their compatibility should be
38 considered. If they cannot be satisfactorily represented together, separate figures can be the solution.
39 Please also note that this essay has not examined statistics such as linear relationships. The methods
40 discussed in the current essay may not apply for other types of visualizations.

References

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